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ABSTRACT

Vintage Capital and Expectations Driven Business Cycles*

This paper demonstrates that increased optimism about future productivity can generate an immediate economic expansion in a neoclassical model with vintage capital and variable capacity utilization. Previous research has documented that standard neoclassical models cannot generate a simultaneous increase in consumption, investment, and hours in response to news shocks, and that optimism in these models tends to reduce investment and hours. When technology is vintage specific, however, expectations of higher future productivity raise the demand for new vintages of capital relative to installed capital. Capital depreciates faster when utilization is high, but this depreciation only affects installed capital. The cost of high depreciation therefore falls when the value of installed capital falls. It is demonstrated here that with standard parameter values, more optimism raises utilization, consumption, investment, hours, and output.

JEL Classification: E13 and E32

Keywords: business cycles, capital-embodied technological change, expectations, news and vintage capital

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1 Introduction

Optimism and pessimism in the economy are often mentioned as important sources of business cycle fluctuations. While traditional Keynesian business cycle theories typically were vague about the sources of demand fluctuations and did not explicitly model expectations, more recent theories (starting with Diamond, 1980, and Cooper and John, 1988) allowed for expectations that were rational but still not related to fundamental developments in the economy. Recent studies, however, have highlighted the importance of information or expectations about fundamental developments and argued that changes in such expectations are related to business cycle fluctuations. In particular, Beaudry and Portier (2006) find that technological developments are reflected in stock market prices several years before the developments can be measured in production data.¹

An important empirical business cycle regularity is that consumption, investment, and employment are procyclical, i.e. that they are positively correlated with output. If changing expectations are an important source of business cycle fluctuations, a theory of the business cycle should be able to generate such positive comovements in response to changing expectations. In a recent paper, however, Beaudry and Portier (2005) demonstrate that shocks that affect expectations but not the current technology cannot generate positive comovements between consumption, employment, and investment in typical neoclassical models.² Using their terminology, these models cannot explain Expectations Driven Business Cycles.

Beaudry and Portier then show that Expectations Driven Business Cycles can be generated in neoclassical settings if there are more than two production sectors and if there are cost complementarities for firms that supply goods to several sectors. In a related paper, Jaimovich and Rebelo (2006) show that changing expectations can generate business cycle fluctuations in a neoclassical model with variable capital utilization, a particular form of adjustment costs for capital, and a particular utility function with a low wealth effect on labor supply. In another recent paper Christiano, Motto and Rostagno (2006) add sticky nominal prices and an inflation targeting central bank to a framework with habit persistence and adjustment costs, and demonstrate that expectations then generate larger and longer fluctuations.

This paper demonstrates that Expectations Driven Business Cycles can be generated in a neoclassical growth model that is more standard than those previously proposed. This model has standard preferences and only one production sector, but adds two realistic and commonly used features to the most basic model. The two additions are variable capital utilization and capital-embodied technological change (or more loosely "vintage capital").³ These model ingredients were proposed already by Greenwood, Hercowitz and

¹Focusing more directly on innovations and diffusion, Rogers (2003) demonstrates that technological innovations indeed diffuse slowly into production.

²This problematic reaction to news was noted earlier by Cochrane (1994), Danthine, Donaldson and Johnsen (1998) and Manuelli (2000). Based on evidence in Rogers (2003), Rotemberg (2003) uses a process where technology diffuses slowly, and again finds that innovations according to the model reduce hours and output on impact.

³Although not crucial in their setting, Jaimovich and Rebelo (2006) also allow for vintage capital, but with a slightly different interpretation that results in a difference in the timing convention. The model used here is therefore almost identical to Jaimovich and Rebelo's, but with standard preferences (following

Huffman (1988) and have since been used widely in the business cycle literature. In their survey of the real business cycle literature, King and Rebelo (1999) argue that variable capital utilization is both a realistic and important ingredient in business cycle models. Greenwood, Hercowitz and Krusell (1997, 2000) further analyze the implications of capital-embodied technological change in neoclassical settings, and Fisher (2005) finds that U.S. business cycle fluctuations are generated by investment-specific technological innovations to a larger extent than by neutral innovations.

To understand why vintage capital and variable utilization are important, consider the most basic neoclassical model. The essence of the argument is best understood if we first abstract from labor supply. Suppose that there are positive news about future productivity but that today's technology is unaffected. Production is then initially fixed so if consumption increases, investment must fall, and if investment increases consumption must fall. By allowing for variable capital utilization, it is possible to raise both consumption and investment even if the technology and the capital stock are fixed. But Beaudry and Portier (2005) show that the planner would never choose to simultaneously raise consumption and investment in typical neoclassical models. That would require higher utilization which would result in higher depreciation of capital. There is therefore still a trade-off between higher consumption today and a higher capital stock tomorrow.

This trade-off is relaxed when the technology is vintage specific. Consider a planner who receives positive news about the future productivity of capital built today. As before, the positive news raises demand both for investment and consumption. But higher capital utilization, implying faster depreciation of installed capital, is now less costly since installed capital will not benefit from the higher future productivity. The planner may therefore choose to simultaneously raise investment (to benefit from high future productivity) and consumption (because of the wealth effect) by utilizing old capital more intensively.

Most previous studies of news shocks in neoclassical settings (for example Cochrane 1994 and Danthine et al. 1998) have concluded that the theory predicts that positive news about future productivity results in lower production and fewer hours worked today. The intuition behind this result is clear; future labor productivity and income is expected to be high so the wealth effect tends to raise consumption and leisure on impact. The value of future capital also increases and this could result in higher labor supply, but the former mechanism typically dominates. An exception is Greenwood, Hercowitz and Huffman (1988). They use a utility function where there are no wealth effects on labor supply, and demonstrate that hours worked then rise in response to positive news because a higher capital utilization rate raises the marginal productivity of labor. They also argue but never explicitly demonstrate that consumption and investment may increase simultaneously in response to positive news. The present paper uses a similar economic environment but demonstrates that Expectations Driven Business Cycles can be generated even with standard preferences that allow for wealth effects on labor supply.

The next section presents the full dynamic model and discusses how it differs from the frameworks analyzed by Beaudry and Portier (2005) and Jaimovich and Rebelo (2006). Section 3 then analyzes a two-period version of the model and demonstrates that Expectations Driven Business Cycles (EDBC) are generated if capacity utilization and labor supply

King, Plosser and Rebelo, 1988), and without adjustment costs for capital.

are sufficiently elastic, and if the depreciation rate of capital is sufficiently high. EDBC can be generated even if labor supply is perfectly inelastic, but only if the intertemporal elasticity of substitution is smaller than unity.⁴ However, EDBC cannot be generated if capacity utilization is perfectly inelastic or if technological innovations are neutral rather than embodied. Section 4 provides numerical examples based on the full dynamic model. These examples demonstrate that EDBC are generated when the model is calibrated with standard parameter values. The examples also support the theoretical results from the two-period model; EDBC are stronger and more likely if capacity utilization and labor supply are more elastic, if the intertemporal elasticity of substitution is low, and if the depreciation rate of capital is high. Section 5 concludes.

2 The Model

2.1 Production and Capital

Consider an economy where the productivity of capital is vintage specific so that capital first used in production in period t has productivity q_t in all periods.⁵ Production is of the Cobb-Douglas form,

$$y_t = \left(\sum_{s=0}^{\infty} u_t q_{t-s} k_{t,s} \right)^{\theta} h_t^{1-\theta},$$

where $k_{t,s}$ denotes the capital introduced in period $t-s$ that is still available in period t , h denotes labor supply, i investment, u the capital utilization rate, and θ the capital share in production.

The vintages of capital develop according to

$$k_{t+1,0} = i_t, \tag{1}$$

and, for $s \geq 1$,

$$k_{t+1,s} = [1 - d(u_t)] k_{t,s-1}. \tag{2}$$

The depreciation rate d depends on capital utilization, and we assume that $d(u)$ is strictly increasing and convex.

The production side of this economy can be formulated more compactly if we let k_t denote the sum of all efficiency units of capital available for production in period t ,

$$k_t = \sum_{s=0}^{\infty} q_{t-s} k_{t,s}, \tag{3}$$

so that

$$y_t = (u_t k_t)^{\theta} h_t^{1-\theta}.$$

⁴When labor supply is inelastic, I define EDBC as a simultaneous increase in consumption and investment in response to an expectational shock.

⁵The technology is thus embodied in the different vintages of capital, and these models are often referred to as models with capital-embodied technological change (see Greenwood, Hercowitz and Krusell, 1997).

Note that (1) and (2) together with (3) imply that⁶

$$k_{t+1} = [1 - d(u_t)] k_t + q_{t+1} i_t. \quad (4)$$

2.2 Households

The economy is populated by a large number of identical households with expected lifetime utility

$$E_0 \sum_{t=0}^{\infty} \beta^t U(c_t, h_t)$$

where c is consumption. The instantaneous utility function belongs to the class of utility functions that King, Plosser and Rebelo (1987) demonstrate is consistent with balanced growth, i.e.

$$U(c, h) = \frac{[cv(h)]^{1-\mu} - 1}{1-\mu}$$

where $\mu > 0$, $v > 0$, $v_h < 0$, $v_{hh} < 0$, and $-\mu v v'' > (1 - 2\mu)(v')^2$. When $\mu \rightarrow 1$ this utility function becomes $U(c, h) = \ln c + \ln v(h)$.

The planner maximizes the households' expected utility subject to the resource constraint

$$c_t + i_t = y_t,$$

the production function

$$y_t = (u_t k_t)^\theta h_t^{1-\theta},$$

and the evolution of efficient capital, equation (4).

2.3 Interpretation

In the present setting different vintages of capital have different productivity in production. Greenwood, Hercowitz and Krusell (1997) however note that this setting is identical to one where all vintages of capital are equally productive, but where the cost of producing the different vintages of capital varies. The term q in equation (4) can therefore either be interpreted as the productivity of the new vintage of capital or as the efficiency in production of investment goods. The timing of information about q may however differ for these two interpretations. It is natural to assume that much information is available about the present production function. If focus is on the latter interpretation, as in and Jaimovich and Rebelo (2006), equation (4) will be replaced by

$$k_{t+1} = [1 - d(u_t)] k_t + q_t i_t$$

⁶Greenwood, Hercowitz and Krusell (1997) start from this specification and interpret q as the productivity of investments. They show in an appendix that the vintage capital interpretation is analytically identical.

where k is raw capital and q_t is known in the beginning of period t . If, as in the present setting, technologies are vintage specific, a natural interpretation is that the productivity of new capital is not perfectly observed until the capital is implemented in production.⁷

Note that the model falls outside the class of models analyzed by Beaudry and Portier (2005). They require that the resource constraint can be written as

$$c_t = G(k_t, h_t, k_{t+1}; q_t)$$

where G is some function (that can include the optimal utilization u_t), and where the variables k_t , h_t , k_{t+1} , and q_t are known or determined in period t . In the present model, however, tomorrow's effective capital stock k_{t+1} depends on tomorrow's productivity q_{t+1} , and the optimal utilization of capital depends on expectations about future productivity.

3 A Two-Period Model

Let us now examine under what conditions Expectations Driven Business Cycles can arise in a two-period version of the model above. Capital utilization is variable in the first period but fixed at unity in the second period, and uncertainty is ignored so that future productivity q_2 is known already in the first period.⁸ The planner solves

$$\max \frac{[c_1 v(h_1)]^{1-\mu} - 1}{1-\mu} + \beta \frac{[c_2 v(h_2)]^{1-\mu} - 1}{1-\mu}$$

subject to

$$c_1 + i_1 = (u_1 k_1)^\theta h_1^{1-\theta} \quad (5)$$

$$c_2 = k_2^\theta h_2^{1-\theta} \quad (6)$$

$$k_2 = [1 - d(u_1)] k_1 + q_2 i_1 \quad (7)$$

$$d(u_1) = \delta + \alpha (u_1^\eta - 1)$$

with k_1 given and assuming $\eta > 1$, $\alpha > 0$, and $0 \leq \delta \leq 1$.⁹

Without loss of generality, we can set $k_1 = 1$ and choose parameter values in the utility function v so that when $q_2 = 1$ we get $u_1 = h_1 = 1$, which also implies that the depreciation rate is δ . The solution to this problem can then be characterized by equation (7) and the following five equations¹⁰

$$h_1^{\mu\theta(\eta-1)\omega} v_1^{1-\mu} = \sigma^\mu \Omega k_2^{-\psi} q_2^{1+\mu\theta\omega} \quad (8)$$

$$c_1 = (1 - \theta) \sigma q_2^{\theta\omega} h_1^{-\theta(\eta-1)\omega} \quad (9)$$

⁷Greenwood, Hercowitz and Huffman (1988) however assume that the productivity of capital first used in period $t + 1$ is known in the beginning of period t .

⁸Investment is furthermore restricted to be non-negative, which implies that second-period consumption equals second-period production.

⁹We let v_t denote $v(h_t)$ and v_{ht} and v_{hht} denote the first and second derivatives of $v(h_t)$ with respect to h_t , etc.

¹⁰See Flodén (2006) for further details on the derivations.

$$i_1 = [h_1 - (1 - \theta) \sigma] q_2^{\theta \omega} h_1^{-\theta(\eta-1)\omega} \quad (10)$$

$$u_1 = q_2^\omega h_1^{(1-\theta)\omega} \quad (11)$$

and

$$h_2 = \frac{-(1 - \theta) v_2}{v_{h_2}}, \quad (12)$$

where we let $\omega = (\eta - \theta)^{-1}$, $\psi = 1 + \theta(\mu - 1)$, $\sigma = -v_1/v_{h_1}$, and $\Omega = \beta\theta(1 - \theta)^\mu \left(h_2^{1-\theta} v_2\right)^{1-\mu}$.

The first equation, the Euler equation, determines first-period hours as a function of future productivity, q_2 , and parameters. The following equations then determine first-period consumption, investment, and capacity utilization as functions of h_1 , q_2 , and parameters. Finally, equation (12) shows that second-period hours worked only depend on the utility function v and the capital share in production.

3.1 Expectations Driven Business Cycles

Suppose that the economy is in an equilibrium where productivity is expected to be constant at unity ($q_2 = 1$) when these expectations become more optimistic (expectations of q_2 rise in the beginning of period 1). We now analyze conditions under which such an increase in optimism can generate an economic expansion and raise consumption, investment, and hours.

Totally differentiate (8) at $h_1 = q_2 = 1$ to get

$$h_q = \frac{dh_1}{dq_2} = \frac{N}{D}$$

where

$$N = (1 + \mu\theta\omega) k_2 + \omega\psi(\theta - \eta i_1), \quad (13)$$

$$D = \left[\frac{\mu - 1 - \mu\sigma_h}{\sigma} + \mu\theta(\eta - 1)\omega \right] k_2 + \psi [1 - \theta(1 - \theta)\omega - (1 - \theta)\sigma_h - \theta(\eta - 1)\omega i_1], \quad (14)$$

and $\sigma_h = -(1 + \sigma v_{hh}/v_h) < 0$. The denominator D is always positive. To see this, note that concavity of the utility function implies that $\mu - 1 - \mu\sigma_h > 0$, and $c_1 > 0$ implies that $i_1 < 1$.

From (11) it is clear that capacity utilization will rise in response to higher future productivity if this productivity increase raises hours worked (i.e. if $h_q > 0$). To see how consumption and investment are affected, totally differentiate (9) and (10) to get

$$c_q = \frac{dc_1}{dq_2} = \theta\omega c_1 + [(1 - \theta)\sigma_h - \theta(\eta - 1)\omega c_1] h_q \quad (15)$$

and

$$i_q = \frac{di_1}{dq_2} = \theta\omega i_1 + [1 - (1 - \theta)\sigma_h - \theta(\eta - 1)\omega i_1] h_q. \quad (16)$$

The model is consistent with expectations driven business cycles (EDBC) if h_q , c_q and i_q are positive. Propositions 1–3 below demonstrate conditions under which EDBC are

generated, and conditions under which EDBC cannot be generated.¹¹ Proposition 1 first demonstrates that any parameterization of the model will generate EDBC if the utility function is separable in consumption and leisure ($\mu = 1$) and the depreciation rate of capital is sufficiently high. The proposition further demonstrates that EDBC can be generated for a broader set of depreciation rates if labor supply and capacity utilization are more elastic. For Proposition 1, it will be useful to define $\gamma = -\sigma_h/\sigma$ and note that $\gamma > 0$, and that γ is the inverse of the Frisch labor supply elasticity when $\mu = 1$.¹²

Proposition 1 *If $\mu = 1$, then*

(a) *for any parameter values $(\beta, \gamma, \eta, \theta)$ that result in $i_1 > 0$, there is a $\delta^* < 1$ such that EDBC are generated for all $\delta > \delta^*$.*

(b) *less elastic labor supply ($\gamma \uparrow$) and less elastic capacity utilization ($\eta \uparrow$) make δ^* more restrictive,¹³*

$$\frac{\partial \delta^*}{\partial \gamma} \Big|_{\delta^* > 0} > 0$$

and

$$\frac{\partial \delta^*}{\partial \eta} \Big|_{\delta^* > 0} > 0$$

(c) *EDBC do not exist if either labor supply or capacity utilization is infinitely inelastic*

$$\lim_{\gamma \rightarrow \infty} \delta^* = \lim_{\eta \rightarrow \infty} \delta^* = 1.$$

To understand why a high depreciation rate facilitates the generation of Expectations Driven Business Cycles in part (a) of Proposition 1, note that hours and investment rise in response to positive news irrespective of the depreciation rate (see the proof of Proposition 1), but that consumption may fall if the depreciation rate is too low. When the depreciation rate increases, second-period production relies to a larger extent on new capital, and the technological development then affects a larger fraction of the capital stock. The wealth effect of positive news therefore becomes more important when depreciation is high, and this tends to raise the reaction of consumption (and reduce the reaction of hours). The intuition behind part (b) of the proposition is more intuitive. In the extreme case when both labor and utilization are perfectly inelastic, it is impossible for consumption and investment to simultaneously rise in response to positive news that does not affect the current technology.

Part (c) of Proposition 1 indicates that elastic capacity utilization and elastic labor supply are important for the existence of EDBC. Proposition 2 demonstrates that elastic capacity utilization is indeed a necessary condition for EDBC in this framework, while Proposition 3 demonstrates that elastic labor supply is not necessary; if $\mu > 1$, EDBC are generated if

¹¹The proofs of these propositions are in the appendix.

¹²The Frisch labor supply elasticity is defined as $wdh/(hdw)|_{u_c}$, i.e. the elasticity of labor with respect to the wage holding marginal utility fixed.

¹³The first part of this statement and the first part of the statement in part (c) of the proposition require that γ can be treated as a parameter. This will be the case for some standard utility functions, for example the one used in Section 4.

capacity utilization is sufficiently elastic (low η) and depreciation sufficiently high. If labor supply is fixed and $\mu \leq 1$, however, EDBC cannot be generated. To understand this, note that a low μ implies a high intertemporal elasticity of substitution. In particular, when $\mu < 1$, the substitution effect dominates over the wealth effect and households are willing to reduce present consumption in exchange for higher future consumption in response to optimistic news.

Proposition 2 *EDBC cannot be generated if capacity utilization is exogenously fixed.*

Proposition 3 *EDBC cannot be generated if labor supply is exogenously fixed and $\mu \leq 1$. If labor supply is exogenously fixed then for any $\mu > 1$ there is a pair (δ^*, η^*) such that all $\delta > \delta^*$ and $\eta < \eta^*$ generate EDBC.*

To better understand the importance of vintage capital, let us consider a specification that nests normal and embodied technological change by replacing (7) with

$$k_2 = \left[(1 - d(u_1)) k_1 + q_2^\phi i_1 \right] q_2^{1-\phi} \quad (7')$$

where $\phi \in [0, 1]$ is the degree of embodiedness. The equations characterizing the solution then change to

$$h_1^{\mu\theta(\eta-1)\omega} v_1^{1-\mu} = \sigma^\mu \Omega k_2^{-\psi} q_2^{\phi(1+\mu\theta\omega)} \quad (8')$$

$$c_1 = (1 - \theta) \sigma q_2^{\phi\theta\omega} h_1^{-\theta(\eta-1)\omega} \quad (9')$$

$$i_1 = [h_1 - (1 - \theta) \sigma] q_2^{\phi\theta\omega} h_1^{-\theta(\eta-1)\omega} \quad (10')$$

and

$$u_1 = q_2^{\phi\omega} h_1^{(1-\theta)\omega}. \quad (11')$$

The importance of embodied technological change is directly indicated in equation (11'); utilization is not affected by expectations of q_2 if technological change is neutral and labor supply is perfectly inelastic. When technological change is embodied, however, expectations of future technological improvements raise utilization.

We are interested in comparing the effects of changes in q_2 for different degrees of embodiedness. Note however that the direct effect of shocks to expected productivity will depend on the degree of embodiedness. In particular, a given increase in q_2 has a larger impact on the second-period efficient capital stock if technology is neutral, since then both old and new capital benefits from the technological improvement. To analyze technological changes with similar immediate effects, let $q_2 = q + m(\phi)\varepsilon$ where $m(\phi) = i_1 / [i_1 + (1 - \phi)(1 - \delta)]$. Then $\partial k_2 / \partial \varepsilon$ is independent of ϕ if we fix i_1 and u_1 , and evaluate derivatives at $q = 1$ and $\varepsilon = 0$. Totally differentiating (8') we then get

$$h_\varepsilon = \frac{dh_1}{d\varepsilon} = \frac{m(\phi)n(\phi)}{D} \quad (17)$$

where the denominator is still given by (14) and where

$$n(\phi) = \phi N - (1 - \phi)\psi k_2. \quad (18)$$

From (9') and (10') we further get

$$c_\varepsilon = \frac{dc_1}{d\varepsilon} = \phi m(\phi) \theta \omega c_1 + [(1 - \theta) \sigma_h - \theta(\eta - 1) \omega c_1] h_\varepsilon \quad (19)$$

and

$$i_\varepsilon = \frac{di_1}{d\varepsilon} = \phi m(\phi) \theta \omega i_1 + [1 - (1 - \theta) \sigma_h - \theta(\eta - 1) \omega i_1] h_\varepsilon. \quad (20)$$

Proposition 4 summarizes some results derived from these equations in the subsequent discussion.

Proposition 4

- (a) Positive news about future productivity reduces hours ($h_\varepsilon < 0$) and investment ($i_\varepsilon < 0$) and raises consumption ($c_\varepsilon > 0$) when technological change is neutral ($\phi = 0$).
- (b) More embodiedness ($\phi \uparrow$) raises the response of hours to positive news shocks ($\partial h_\varepsilon / \partial \phi > 0$).

When technological change is neutral, the model falls into the class of models analyzed by Beaudry and Portier (2005) and consequently h_ε , i_ε , and c_ε can then not simultaneously be positive. That result is confirmed here, and we can make a stronger statement: in the basic neoclassical model with neutral technological change ($\phi = 0$) and standard preferences (as in King, Plosser and Rebelo, 1988), positive news about future productivity raises consumption but reduces labor supply and investment on impact. This statement follows since $D > 0$ and since equation (18) implies that $n(0) < 0$ and consequently $h_\varepsilon < 0$ when $\phi = 0$. Furthermore, $1 - (1 - \theta) \sigma_h - \theta(\eta - 1) \omega i_1 > 0$ implies that $i_\varepsilon < 0$ when $h_\varepsilon < 0$ while $\sigma_h < 0$ implies that $c_\varepsilon > 0$ if $h_\varepsilon < 0$, all under the assumption that $\phi = 0$.

Fisher (2005) finds that hours respond more strongly to investment specific shocks than to neutral shocks that immediately raise productivity. A similar result holds in the present framework. Differentiating equation (17) we get $\partial h_\varepsilon / \partial \phi > 0$, i.e. hours respond more strongly to embodied technological shocks than to neutral news shock. Intuitively, present leisure is more expensive relative to future leisure when technology is embodied so that only new investments benefit from the technological developments.

One may suspect that a similar argument implies that consumption is less responsive to embodied technological shocks than to neutral shocks, but that need not be the case. The second term on the right hand side in equation (19) captures the effect that embodiedness reduces the responsiveness of consumption if hours become more responsive. The first term is however more positive if technology is embodied. The key to understanding this effect is equation (11'). If $\phi > 0$, higher future productivity implies higher utilization even if hours are unaffected. The intuition is that the cost of high utilization in terms of high depreciation of installed capital is smaller when installed capital does not benefit from technological improvements. The higher utilization may imply that consumption becomes more responsive to embodied shocks than to neutral shocks, and also reinforces the increase in responsiveness of investment.

4 Numerical Examples

Let us now return to the infinite-horizon model specified in Section 2, and analyze numerically how the economy reacts to changing expectations. Let $v(h) = \exp(-\zeta h^{1+\gamma}/(1+\gamma))$ so that the utility function is¹⁴

$$u(c, h) = \frac{\left[c \exp\left(\frac{-\zeta h^{1+\gamma}}{1+\gamma}\right) \right]^{1-\mu} - 1}{1-\mu}$$

when $\mu \neq 1$ and

$$u(c, h) = \log c - \frac{\zeta h^{1+\gamma}}{1+\gamma}$$

when $\mu = 1$.

Except for the utility function, the parameterization of the model mostly follows Jaimovich and Rebelo (2006). In the benchmark specification, we then have unit risk aversion, $\mu = 1$, and to get a labor supply elasticity of 2.5 we set $\gamma = 1/2.5 = 0.4$. The capital share in production is set to $\theta = 0.36$, and the parameter determining the elasticity of depreciation to utilization is set to $\eta = 1.20$. This choice is rather arbitrary, and alternative values will be considered. Furthermore, one model period is one quarter of a year, and the time-discount factor is set to $\beta = 0.985$. The parameters ζ and α are chosen so that the economy converges to a steady state with $h = u = 1$ when technology is constant at $q = 1$, and we set $\delta = 0.02$ so that the depreciation rate is 2 percent in that steady state. Table 1 summarizes the parameter values used in the benchmark economy, and also reports the implied steady state values for the variables.¹⁵

Table 1: Benchmark Values

Parameter values		Initial steady state	
α	0.0294	u	1.0000
β	0.9850	k	37.7748
γ	0.4000	h	1.0000
δ	0.0200	c	2.9410
ζ	0.8044	i	0.7555
η	1.2000	y	3.6965
θ	0.3600		
μ	1.0000		

4.1 The Economy's Response to News

To examine how the economy reacts to news about future productivity, three experiments are considered. Common to these experiments is that in the beginning of period one the

¹⁴This function is not always concave when $\mu < 1$. Only specifications where $\mu \geq 1$ are therefore considered.

¹⁵See the appendix for a description of the solution to this model.

economy is in a steady state without technological change when agents get unanticipated news that technology will permanently improve by one percent from period two and on, i.e. $q_t = 1.01q_1$ for all $t \geq 2$.

In the first experiment, this new information is correct and technology develops as anticipated. Figure 1 shows how the economy reacts to this technological improvement, and Table 2 reports the impact reaction when the news about future technological improvements arrive. For the benchmark parameterization, the conditions for EDBC are fulfilled; there is an economic expansion already in the first period although the technology is not affected until in the second period. From Table 2 we also see that the response to changing expectations can be quantitatively important. Investment increases by almost four percent and production by almost one percent in the first period when productivity is expected to increase by one percent.

Columns (ii) to (vi) in Table 2 show the impact responses to the news shock under alternative parameterizations. In column (ii), $\gamma = 2.0$ so that the labor-supply elasticity is 0.5. As expected, the impact responses are smaller when labor supply is less elastic. When risk aversion is higher (column (iii)), the willingness to intertemporally substitute is lower and consumption smoothing is more important. Consumption therefore increases faster towards the new equilibrium level and as a consequence the impact response of investment is smaller. The analysis in Section 3 demonstrated that elastic capital utilization is crucial for obtaining a simultaneous first-period increase in consumption and investment. As expected, therefore, the impact responses are smaller when capital utilization is less elastic as in column (iv). The impact response of consumption is then negligible but still positive. Column (iv) indicates that a higher capital share in production raises the impact responses while column (v) indicates that a higher steady-state depreciation rate raises the impact response of consumption but reduces the response of the other variables.

To isolate the effects generated by expectations from those generated by technology, the other experiments hold technology constant. First, suppose that technology does not improve in the second period and that the optimistic news received in the first period then are revised so that $E_2q_t = q_t = q_1$ for all $t \geq 2$. As displayed in Figure 2, there is an expectations generated expansion in the first period, and then the economy quickly returns to the old steady state when expectations are falsified. Second, suppose that expectations in periods $t = 1, 2, \dots, 10$ are that productivity will increase permanently by one percent from next period, i.e. $E_tq_s = 1.01q_t$ for all $s > t$, but that productivity turns out to be constant, i.e. $q_s = q_1$ for all s . Figure 3 shows that most of the adjustment to these expectations comes in the first optimistic period, and that the readjustment when expectations are normalized is again rapid.

Since consumption is always above the true trend, these experiments do not result in a genuine recession when optimistic expectations are normalized. The loss associated with the incorrect expectations are instead generated by inefficiently high labor supply during the expansion. When expectations are normalized, the capital stock is high, and households can enjoy higher consumption and leisure than in the absence of the expansion. An econometrician observing the macroeconomic development will however notice a sharp contraction in economic activity when expectations are normalized.

Table 2: Impact response to news

	Benchmark	$\gamma = 2.0$	$\mu = 2.0$	$\eta = 1.50$	$\theta = 0.40$	$\delta = 0.03$
	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Δc_1	0.16	0.05	0.27	0.00	0.19	0.18
Δh_1	0.55	0.18	0.31	0.56	0.62	0.52
Δi_1	3.94	2.71	2.44	3.87	4.04	3.22
Δu_1	1.61	1.33	1.43	1.20	1.72	1.59
Δy_1	0.93	0.59	0.72	0.79	1.06	0.90

Note: The table shows the percentage change in the variables in response to a one percent permanent increase in q_t , $t \geq 2$, when news about this change arrive in the beginning of period $t = 1$. Column (i) shows the outcome under the benchmark parameterization. The following columns show results under alternative parameterizations.

To further examine the validity of the two-period analysis for the fully dynamic setting, Figure 4 displays combinations of parameter values that generate EDBC. In the first panel, all parameters are held at the benchmark values except the elasticities of capacity utilization and labor supply. When capacity utilization is less elastic (higher η) labor supply must be more elastic (lower γ) for expectations driven business cycles to be generated. This finding is in line with Proposition 1b and Proposition 2. The second panel shows that EDBC can be generated with less elastic labor supply if risk aversion is high, which was also indicated by Proposition 3. The final panel shows that also a high depreciation rate of capital allows for EDBC under less restrictive assumptions of the labor-supply elasticity, as was indicated by Proposition 1a and Proposition 3.

5 Concluding Discussion

This paper has demonstrated that optimism and pessimism of future productivity can generate business cycle fluctuations in a neoclassical growth model with vintage capital and variable capacity utilization. To isolate the mechanisms, only exogenous changes in expectations have been considered, and uncertainty and innovations have not explicitly been modeled. Because of the simplistic treatment of technological development, with only one consumption good and one type of capital, optimism about future technologies that never materialize still result in a high capital stock. More realistically, some innovations or expectations about new technologies generate investments that turn out to be wasted. To fully understand how expectations interact with the business cycle, future work needs to model the processes for technological innovations, the implementation of these innovations in production, and the information and uncertainty about how these innovations affect productivity.

In the present paper, expectations are formed one quarter ahead and investments are transformed into capital in one quarter. The evidence reported both by Rogers (2003) and by Beaudry and Portier (2006) however indicates that technological developments diffuse slowly into production and that news of innovations may affect expectations several years before total factor productivity is affected. A quantitatively more realistic model

specification should therefore allow for a longer lag between information shocks and implementation, maybe by allowing for "time-to-build" as in Kydland and Prescott's (1982) original real business cycle model.

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Appendix A: Proofs of Propositions

A.1 Proof of Proposition 1

Proof. When $\mu = 1$, (13) reduces to

$$N/\omega = \eta(1 - \delta) + \theta$$

and (14) reduces to

$$D/\omega = \theta(\eta - 1)(1 - \delta) + (-\sigma_h/\sigma)(\eta - \theta)(2 - \delta) + \eta - \theta - \theta(1 - \theta).$$

Note that

$$\eta - \theta - \theta(1 - \theta) = \eta - 1 + (1 - \theta)^2 > 0$$

where the inequality follows from our assumption that $\eta > 1$ and $1 > \theta > 0$. Note also that $\sigma > 0$ and $\sigma_h < 0$ since by assumption $v > 0$, $v_h < 0$, and $v_{hh} < 0$. We then see that both N and D are positive, and consequently $h_q > 0$.

From (16) we get

$$\frac{i_q}{\omega} = \theta i_1 + [\eta + (\eta - \theta)(-\sigma_h) + (\eta - 1)\theta\sigma](1 - \theta)h_q$$

which is positive if $h_q > 0$ and $i_1 > 0$.

Equation (15) implies that

$$\frac{c_q}{\omega c_1} = \theta - [\gamma(\eta - \theta) + \theta(\eta - 1)]h_q$$

which in turn implies that

$$\begin{aligned} c_q &> 0 &\iff \theta - [\gamma(\eta - \theta) + \theta(\eta - 1)]h_q > 0 \\ &\iff \phi < \theta \end{aligned}$$

where we define

$$\phi = \frac{[\gamma(\eta - \theta) + \theta(\eta - 1)][\eta(1 - \delta) + \theta]}{\theta(\eta - 1)(1 - \delta) + \gamma(\eta - \theta)(2 - \delta) + \eta - \theta - \theta(1 - \theta)}.$$

We can then derive

$$\phi < \theta \iff \delta > \delta^* = 1 - \frac{\theta(1 - \theta)}{\gamma(\eta - \theta) + \theta(\eta - 1)}. \quad (\text{A.1})$$

This demonstrates part (a) of the proposition, i.e. for any parameter values $(\beta, \gamma, \eta, \theta)$ there is a $\delta^* < 1$ such that all $\delta > \delta^*$ result in EDBC.

Taking derivatives of δ^* as defined in (A.1) we get

$$\frac{\partial \delta^*}{\partial \gamma} = \frac{(\eta - \theta)(1 - \delta^*)}{\gamma(\eta - \theta) + \theta(\eta - 1)}$$

and

$$\frac{\partial \delta^*}{\partial \eta} = \frac{(\gamma + \theta)(1 - \delta^*)}{\gamma(\eta - \theta) + \theta(\eta - 1)}.$$

If $\delta^* > 0$, both these derivatives are positive, which demonstrates part (b) of the proposition.

From (A.1) it is also clear that

$$\lim_{\gamma \rightarrow \infty} \delta^* = \lim_{\eta \rightarrow \infty} \delta^* = 1$$

which demonstrates part (c) of the proposition. ■

A.2 Proof of Proposition 2

When $\eta \rightarrow \infty$, equation (9) reduces to

$$c_1 = (1 - \theta) \sigma h_1^{-\theta}.$$

Totally differentiating we get

$$c_q = [(1 - \theta) \sigma_h - \theta c_1] h_q.$$

Since $\sigma_h < 0$, we see that c_q and h_q have different signs, and consequently cannot simultaneously be positive.

A.3 Proof of Proposition 3

Proof. If labor supply is fixed at $h_1 = h_2 = 1$, the equilibrium is characterized by the Euler equation

$$c_1^{-\mu} = \beta \theta q_2 \left[1 - \delta - \alpha (u_1^\eta - 1) + q_2 u_1^\theta - q_2 c_1 \right]^{-\psi} \quad (\text{A.2})$$

and the budget constraint $i_1 = u_1^\theta - c_1$ where capacity utilization is $u_1 = q_2^\omega$. Totally differentiating these equations at an initial equilibrium where $q_2 = u_1 = 1$, we get

$$c_q = \frac{(1 - c_1) \psi - k_2}{\psi + \mu k_2 / c_1} \quad (\text{A.3})$$

and

$$i_q = \frac{\theta}{\eta - \theta} - \frac{dc_1}{dq_2}. \quad (\text{A.4})$$

Note that the denominator in (A.3) is positive. We then get

$$\begin{aligned} c_q > 0 &\iff (1 - c_1) [1 + \theta(\mu - 1)] > k_2 \\ &\iff i_1 [1 + \theta(\mu - 1)] > 1 - \delta + i_1 \\ &\iff \theta(\mu - 1) i_1 > 1 - \delta \end{aligned} \quad (\text{A.5})$$

From (A.5) we immediately see that c_q cannot be positive if $\mu \leq 1$. It remains to show that for any $\mu > 1$, there are parameter values δ and η such that both c_q and i_q are positive.

The proof proceeds in two steps. It is first demonstrated that $c_q > 0$ for sufficiently high δ . It is then demonstrated that $i_q > 0$ for sufficiently low η .

In the initial equilibrium, the Euler equation (A.2) reduces to

$$c_1^{-\mu} = \beta\theta [2 - \delta - c_1]^{-\psi}.$$

Totally differentiating with respect to c_1 and δ , we get $dc_1/d\delta < 0$ and thus $di_1/d\delta > 0$ for any recalibration that holds capacity utilization fixed at $u_1 = 1$. Consequently, for any $\mu > 1$, as δ is raised towards unity, the left hand side of (A.5) becomes larger (starting from a positive value) while the right hand side approaches zero. There is therefore a δ^* such that the inequality is satisfied for all $\delta > \delta^*$.

From (A.4) we get

$$\begin{aligned} i_q > 0 &\iff \frac{\theta}{\eta - \theta} > c_q \\ &\iff \frac{\theta}{\eta - \theta} \left[\frac{\psi}{k_2} + \frac{\mu}{c_1} \right] > \frac{(1 - c_1)\psi}{k_2} - 1 \\ &\iff \left(\frac{\theta\mu}{(\eta - \theta)c_1} + 1 \right) k_2 > [1 + \theta(\mu - 1)] \left(\frac{\eta - 2\theta}{\eta - \theta} - c_1 \right) \end{aligned}$$

Note that

$$k_2 = 1 - \delta + i_1 > i_1 = 1 - c_1 > \frac{\eta - 2\theta}{\eta - \theta} - c_1.$$

Consequently, if

$$\frac{\theta\mu}{(\eta - \theta)c_1} + 1 > 1 + \theta(\mu - 1)$$

then $i_q > 0$ for all $i_1 > 0$. Note that

$$\begin{aligned} \frac{\theta\mu}{(\eta - \theta)c_1} + 1 &> 1 + \theta(\mu - 1) \\ &\iff \frac{\mu}{(\eta - \theta)c_1} > \mu - 1. \end{aligned}$$

If $i_1 > 0$, we have $c_1 < 1$ and thus $\mu/[(1 - \theta)c_1] > \mu > \mu - 1$. There is therefore always a value η^* such that the inequality is fulfilled for all $\eta < \eta^*$. ■

Appendix B: Model Solution

This appendix describes the solution to the model analyzed in Section 4. The relevant first order conditions are

$$U_{h_t} = -(1 - \theta)(u_t k_t)^\theta h_t^{-\theta} U_{c_t} \tag{B.6}$$

$$u_t^{\eta - \theta} = \frac{\theta}{\eta\alpha} \left(\frac{h_t}{k_t} \right)^{1 - \theta} q_{t+1} \tag{B.7}$$

and

$$\beta \left[\theta u_{t+1}^\theta k_{t+1}^{\theta-1} h_{t+1}^{1-\theta} q_{t+2} + (1 - d(u_{t+1})) \right] \frac{U_{c_{t+1}}}{q_{t+2}} = \frac{U_{c_t}}{q_{t+1}}. \tag{B.8}$$

B.1 Steady State

Consider first a steady state where q is constant. This steady state is described by the budget constraint $d(u)k = qi$ and the first order conditions (B.6) to (B.8) which reduce to

$$U_h = -(1 - \theta)(uk)^\theta h^{-\theta} U_c \quad (\text{B.9})$$

$$u^{\eta-\theta} = \frac{\theta}{\eta\alpha} \left(\frac{h}{k}\right)^{1-\theta} q \quad (\text{B.10})$$

and

$$\beta \left[\theta u^\theta k^{\theta-1} h^{1-\theta} q + (1 - d(u)) \right] = 1. \quad (\text{B.11})$$

We want to calibrate the model so that $h = u = 1$ when $q = 1$. By using $k = i/\delta$ in (B.11) we see that the marginal product of efficient capital is $\theta k^{\theta-1} = 1/\beta - 1 + \delta$ so that the efficient capital stock can be calculated as a function of known parameters. Using this expression in (B.10) we get

$$\alpha = \frac{\theta k^{\theta-1}}{\eta} = \frac{1}{\eta} \left(\frac{1}{\beta} - 1 + \delta \right).$$

Calculating U_c and U_h and using those expressions in (B.9) we get $\zeta h^{\gamma+\theta} c = (1 - \theta)(uk)^\theta$. To get $h = 1$ we must therefore have $\zeta c = (1 - \theta)k^\theta$. Note that $c + i = k^\theta$ and $i = \delta k$, which implies that

$$\zeta = \frac{1 - \theta}{1 - \delta k^{1-\theta}}.$$

In a steady state where $q \neq 1$ (B.10) and (B.11) imply that

$$\beta [\eta\alpha u^\eta + (1 - d(u))] = 1$$

which demonstrates that u is unaffected by q in steady state. We thus still have $u = 1$, and using this in (B.10) we get

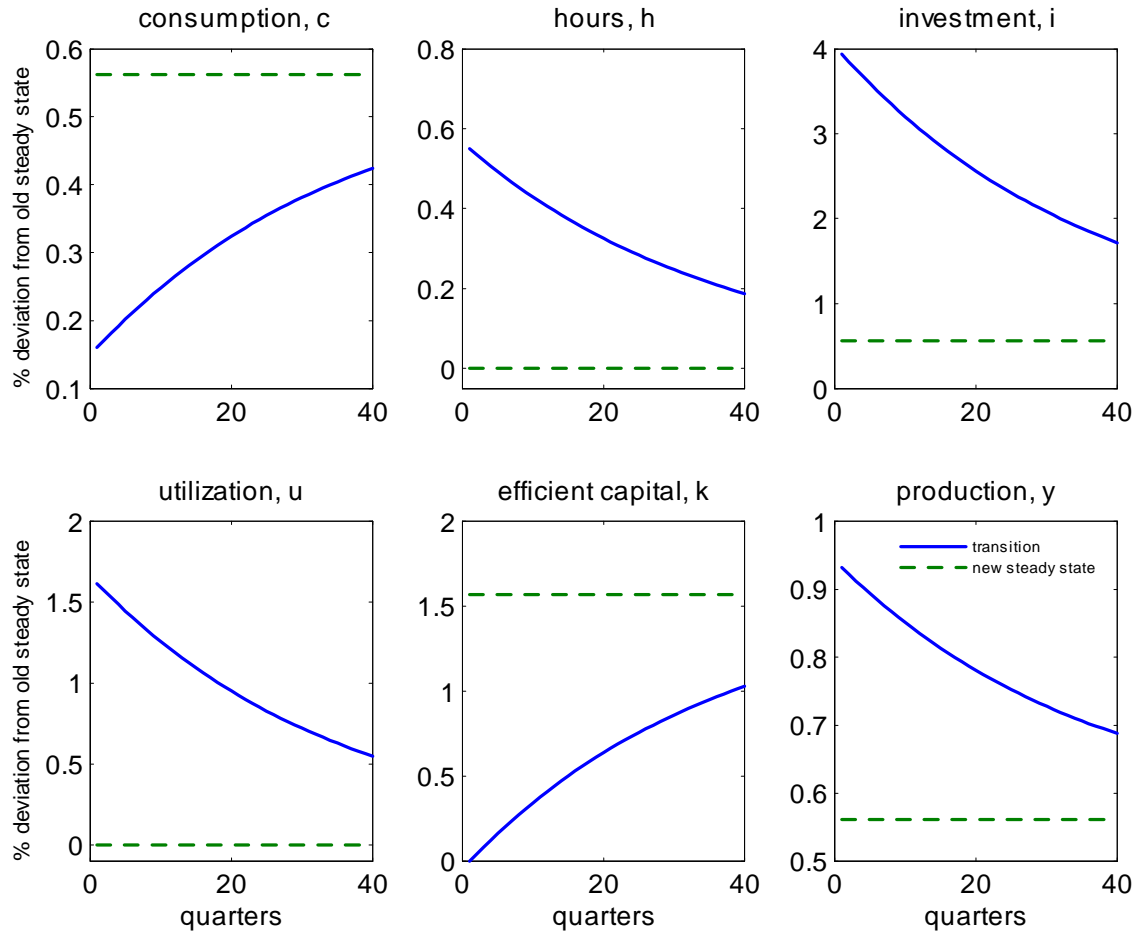
$$k = \left(\frac{\theta q}{\eta\alpha} \right)^{\frac{1}{1-\theta}} h.$$

One can also show that h is also unaffected but this also follows from the properties of the utility function. We thus have $h = 1$ and then $c = (1 - \theta)k^\theta/\zeta$, etc.

B.2 Transition

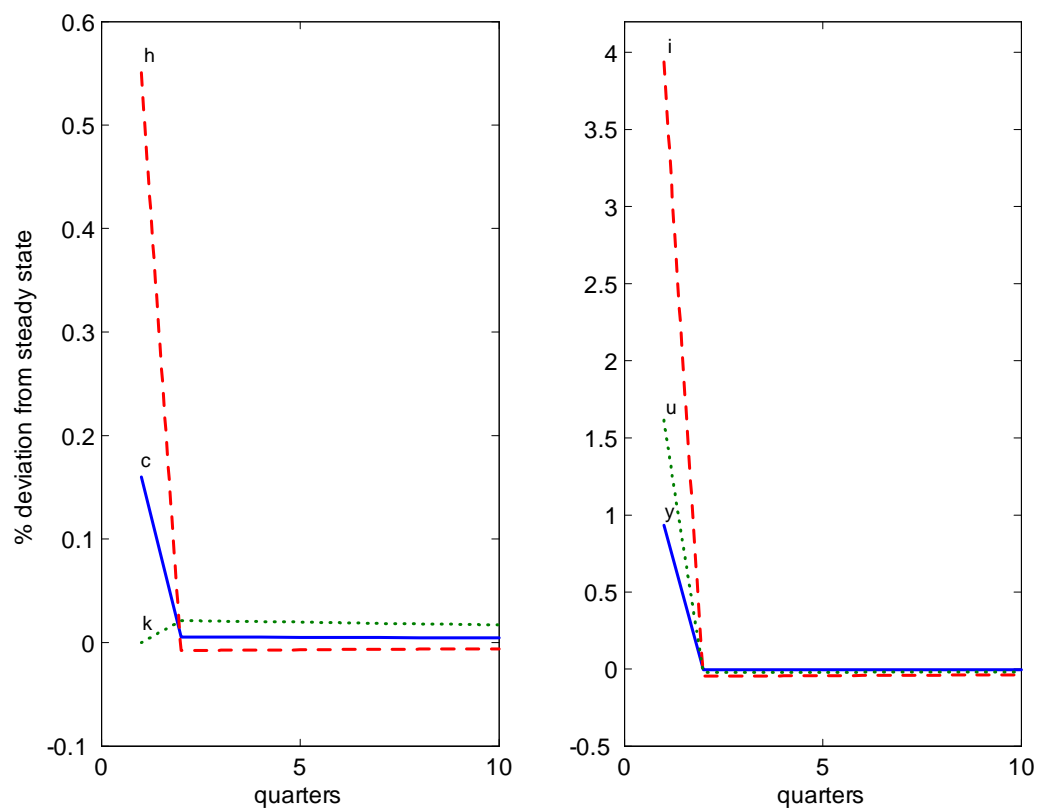
Suppose that the economy is in this steady state in the beginning of period 1, and suppose that agents then learn that from period 2 and on, productivity will be $q_t = \hat{q}$. To solve for the transition to the new steady state, guess some path $\{h_t\}_{t=1}^T$ for some large T . Then follow this procedure: (i) Set $s = 1$. (ii) Use (B.7) to solve for u_s . (iii) Use (B.6) to solve for c_s . (iv) Use the production function to calculate y_s , and use the resource constraint to calculate i_s . (v) Use (4) to calculate k_{s+1} . (vi) Raise s by one, and iterate from (ii) if $s \leq T$. (vii) Use the calculated paths to evaluate the Euler equation (B.8) in all periods. If these equations are not satisfied, use an equation solver to update the guess for $\{h_t\}_{t=1}^T$ and iterate from (i).

Figure 1: Correctly anticipated productivity increase



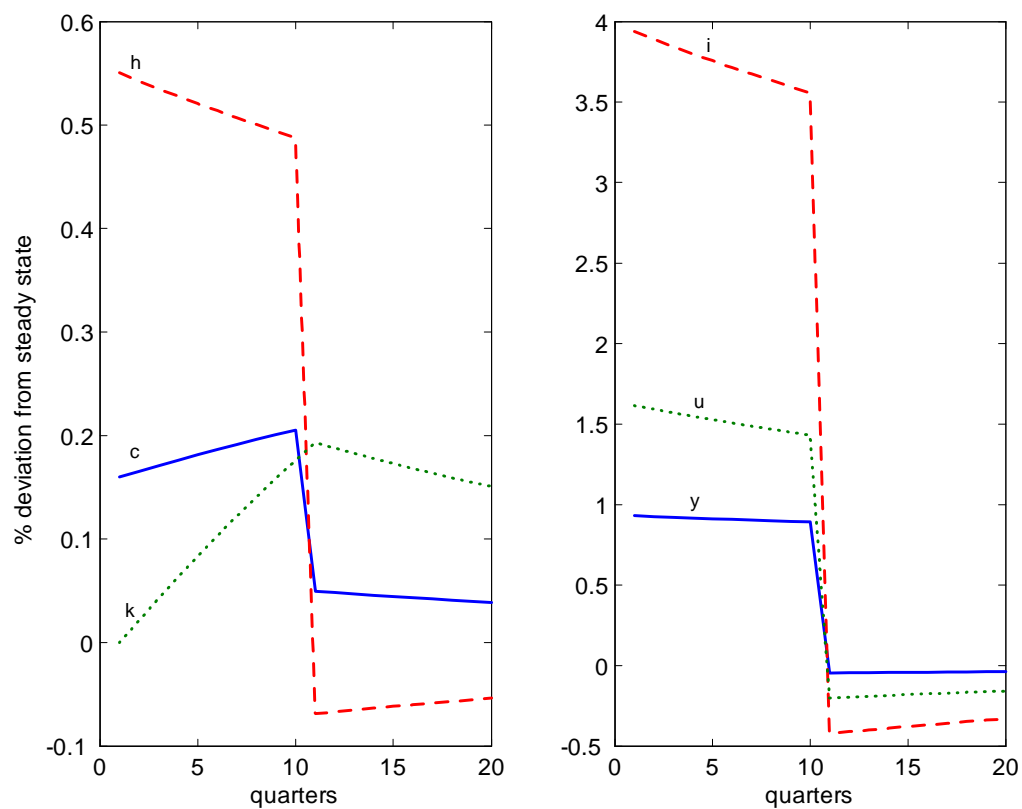
Note: The figure shows the response to a one percent permanent productivity increase in period 2 announced in period 1, i.e. $E_1 q_t = q_t = 1.01q_1$ for $t \geq 2$.

Figure 2: Temporary optimism



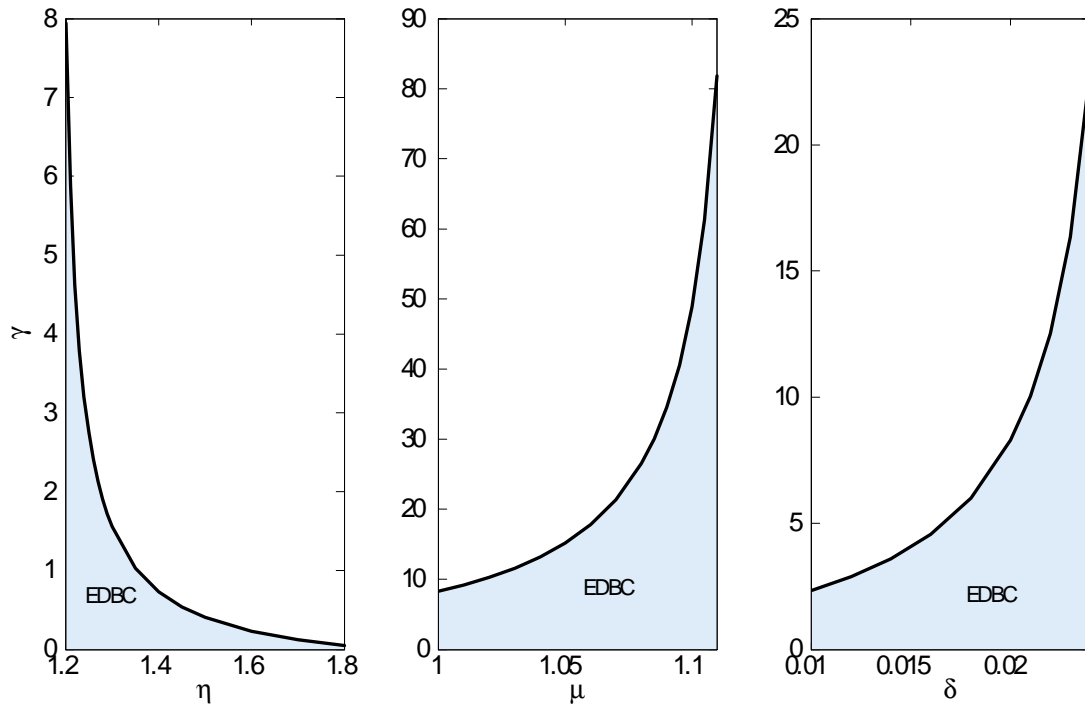
Note: The figure shows the development when agents in period $t = 1$ believe that productivity will increase permanently by one percent from period $t = 2$, but when productivity turns out to be constant, and agents learn this in period $t = 2$.

Figure 3: Repeated optimism



Note: The figure shows the development when productivity is constant ($q_t = 1, \forall t$) but agents repeatedly (in periods 1 to 10) expect productivity to rise permanently by one percent from next period.

Figure 4: Combinations of parameter values that generate EDBC



Note: The shaded areas show combinations (γ, η) , (γ, μ) , and (γ, δ) that generate EDBC when the other parameters are set to the benchmark values.